

Higher Structures

Vertical Forces
 $\Sigma F \uparrow = \Sigma F \downarrow$

Horizontal Forces
 $\Sigma F \rightarrow = \Sigma F \leftarrow$

Moments
 $\Sigma CW M = \Sigma AC W M$

Resolution of a force

$\sin 30^\circ = F_V / 90$
 $F_V = 90 \times \sin 30^\circ$
 $F_V = 45 \text{ N}$

$\cos 30^\circ = F_H / 90$
 $F_H = 90 \times \cos 30^\circ$
 $F_H = 78 \text{ N}$

Resolution of forces on a point

- 1 - Resolve all forces
- 2 - $\Sigma F \uparrow = \Sigma F \downarrow$ to find R_V
- 3 - $\Sigma F \rightarrow = \Sigma F \leftarrow$ to find R_H
- 4 - Pythagoras to find R_A
- 5 - Find the angle ($\tan \alpha = R_V / R_H$)

Moments with a force at an angle

- 1 - Resolve F to find vertical component
- 2 - $\Sigma CW M = \Sigma AC W M$

Simple supports

- 1 - $\Sigma CW M = \Sigma AC W M$ taking moments about R_A to find R_B
- 2 - $\Sigma F \uparrow = \Sigma F \downarrow$ to find R_A

Hinge & Roller

- 1 - Resolve 80N force to find vertical component
- 2 - $\Sigma CW M = \Sigma AC W M$ taking moments about R_A to find R_B
- 3 - $\Sigma F \uparrow = \Sigma F \downarrow$ to find R_{AV}
- 4 - $\Sigma F \rightarrow = \Sigma F \leftarrow$ to find R_{AH}
- 5 - Pythagoras to find R_A
- 6 - Find the angle ($\tan \alpha = R_V / R_H$)

Uniformly Distributed Loads (UDLs)

- 1 - Calculate the UDL (Force x distance)
- 2 - Resolve 5kN force to find vertical component
- 2 - $\Sigma CW M = \Sigma AC W M$ taking moments about R_A to find R_B
- 3 - $\Sigma F \uparrow = \Sigma F \downarrow$ to find R_{AV}
- 4 - $\Sigma F \rightarrow = \Sigma F \leftarrow$ to find R_{AH}
- 5 - Pythagoras to find R_A
- 6 - Find the angle ($\tan \alpha = R_V / R_H$)

Strut
 Members that are in compression, due to external forces trying to compress them, are known as Struts.

Tie
 Members that are in tension, due to external forces trying to pull them apart, are known as Ties.

Nodal analysis

- 1 - Analyse the first node to break down any forces at an angle into horizontal and vertical components.
- 2 - As we know a vertical force at A and only have one unknown vertical AB_V , we start with $\Sigma F \uparrow = \Sigma F \downarrow$ to find AB_V .
- 3 - We can now draw AB as a triangle of forces to use trigonometry and Pythagoras to solve AB and AB_H .
- 4 - Once we know AB_H , we can find AE using $\Sigma F \rightarrow = \Sigma F \leftarrow$.
- 5 - Now using node B we can add the values we already know, remembering that they act the opposite direction at the other end.
- 6 - Start with $\Sigma F \uparrow = \Sigma F \downarrow$ to find BD_V .
- 7 - We can now draw BD as a triangle of forces to use trigonometry and Pythagoras to solve BD and BD_H .
- 8 - Once we know BD_H , we can find BC using $\Sigma F \rightarrow = \Sigma F \leftarrow$.
- 9 - We then complete the table and state whether the member is a Strut (in compression) or a Tie (in tension).

Member	Magnitude	Nature
AB	910 N	Tie
AE	790 N	Strut
BD	1800 N	Strut
BC	2300 N	Tie

Simultaneous Equations

8. (continued)

MARKS

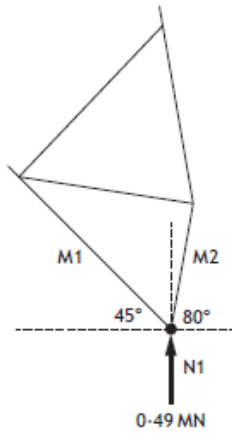
During the design phase a structural engineering company produced detailed information about the internal structure of the Kelpies' steel support legs is shown.

Detail from a proposed design for one of the Kelpies' steel support legs is shown.

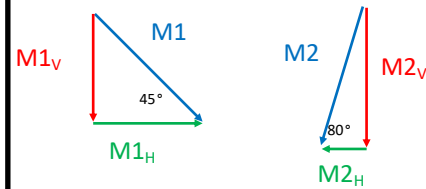
Node N1 is in static equilibrium.

M2 is a strut.

(b) Calculate, using simultaneous equations, the magnitude of the forces in members M1 and M2, and state the nature of the internal force acting on M1.



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$$\sin 45^\circ = \frac{M1_v}{M1} \quad \sin 80^\circ = \frac{M2_v}{M2}$$

$$M1_v = M1 \times \sin 45^\circ \quad M2_v = M2 \times \sin 80^\circ$$

$$M1_v = M1 \times 0.707 \quad M2_v = M2 \times 0.984$$

$$\cos 45^\circ = \frac{M1_h}{M1} \quad \cos 80^\circ = \frac{M2_h}{M2}$$

$$M1_h = M1 \times \cos 45^\circ \quad M2_h = M2 \times \cos 80^\circ$$

$$M1_h = M1 \times 0.707 \quad M2_h = M2 \times 0.173$$

$$\sum F \uparrow = \sum F \downarrow$$

$$0.49 = (M1 \times 0.707) + (M2 \times 0.984)$$

$$\sum F \rightarrow = \sum F \leftarrow$$

$$(M1 \times 0.707) = (M2 \times 0.173)$$

Find the common factor, in this case ($M1 \times 0.707$) and substitute the value into one of the equations to solve M2.

$$0.49 = (M2 \times 0.173) + (M2 \times 0.984)$$

$$0.49 = M2(0.173 + 0.984)$$

$$0.49 = M2 \times 1.157$$

$$\frac{0.49}{1.157} = M2$$

$$M2 = 0.42 \text{ MN}$$

Now substitute the value of M2 into one of the equations to solve for M1.

$$(M1 \times 0.707) = (0.42 \times 0.173)$$

$$M1 \times 0.707 = 0.07266$$

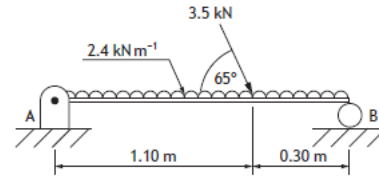
$$M1 = \frac{0.07266}{0.707}$$

$$M1 = 0.1 \text{ MN}$$

7. Viewing platforms are commonplace in sports academies to allow for filming of training and games.



A beam used in the construction of the viewing platform is shown.



(a) (i) Calculate the magnitude of the reaction at B.

3

7. (a) (continued)

(ii) Calculate the magnitude and direction of the reaction at A.

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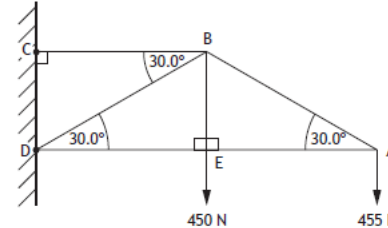
1 mark for UDL point load equivalent (no unit required).	3	UDL = 2.4×1.4 CWM = ACWM (3.36×0.7) + ($3.5 \sin 65^\circ \times 1.1$) = $B \times 1.4$ B (vertical) = 4.172346414 = 4.2 kN (2 sf)
1 mark for calculating B with correct unit.	4	$\sum F_v = 0$ $3.5 \cos 65^\circ = H_A = 1.479163916$ $H_A = 1.479163916 \text{ kN}$ Node B $\sum F_H = 0$ $3.5 \sin 65^\circ = H_B = 1.479163916$ $H_B = 1.479163916 \text{ kN}$ Node B $\sum F_v = 0$ $R_B = 2.761613697 + 1.479163916$ $R_B = 4.240777613$ $R_B = 4.2 \text{ kN}$ (2 sf)
1 mark for calculating R_B with correct unit.	1	$\theta = \tan^{-1}(\frac{3.32077255}{2.761613697})$ $\theta = 50.8^\circ$ (2 sf)
1 mark for calculating direction with correct unit.	1	$\theta = 50.8^\circ$ (2 sf)

8. (continued)

Due to the rapid expansion of the construction site, additional floodlights are to be installed.



The diagram below shows part of the design for the frame that supports the floodlights.



(c) Calculate, using nodal analysis at nodes A and B, the magnitude and nature of the forces in members AB, AE, BD, and BC.

Member BE is a 450 N tie.

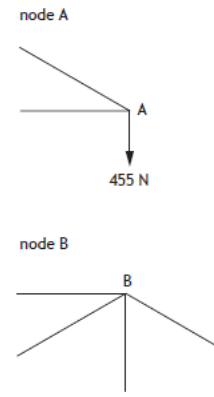
Complete the table below. Show all working and final units.

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Member	Magnitude	Nature
AB		tie
AE		strut
BD		
BC		

8. (c) (continued)

Space for calculations

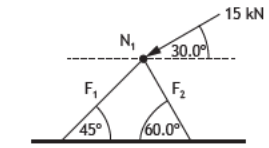


1 mark for presentation of equation shown is acceptable.	1	$\sum F_v = 0$ $F_{AB} \sin 30^\circ + F_{BC} \cos 60^\circ = 15 \cos 30^\circ$
1 mark for equation based on vertical force components.	1	$F_{AB} \sin 45^\circ = 15 \sin 30^\circ + F_{BC} \sin 60^\circ$
1 mark for equation based on horizontal force components.	1	$F_{AB} \cos 45^\circ + F_{BC} \cos 60^\circ = 15 \cos 30^\circ$
1 mark for F_1 with correct unit.	1	$F_1 = 16 \text{ kN}$ (2 sf)
1 mark for F_2 with correct unit.	1	$F_2 = 4.0 \text{ kN}$ (2 sf)
1 mark for appropriate substitution (other correct methods are acceptable).	1	$F_2 = (1.5 \sin 30^\circ - 15 \cos 30^\circ) / (-\sin 60^\circ - \cos 60^\circ)$ $F_2 = (-1.5 \sin 60^\circ - 15 \cos 60^\circ) / (-\sin 60^\circ - \cos 60^\circ)$ $F_2 = 4.0 \text{ kN}$ (2 sf)
1 mark for F_1 with correct unit.	1	$F_1 \sin 45^\circ - 4.0 \sin 60^\circ = 15 \sin 30^\circ$ $F_1 = 15.5055812$ $F_1 = 16 \text{ kN}$ (2 sf)
1 mark for nature.	1	BC is a tie
1 mark for BC.	1	BC = 2300 N (2 sf)
1 mark for substitution.	1	BC = $1800 \cos 30^\circ + 910 \cos 30^\circ$ BC = 2346.928844
1 mark for nature.	1	BD is a strut
1 mark for BD.	1	BD = 1800 N (2 sf)
1 mark for substitution.	1	BD = 1810 N BD = $910 \sin 30^\circ + 450$
1 mark for AE.	1	AE = 790 N (2 sf)
1 mark for AB.	1	AB = 910 N (2 sf)
1 mark for presentation of equation shown is acceptable.	1	Node A $\sum F_v = 0$ AB = 910 N (2 sf)
1 mark for equation based on horizontal force components.	1	Node B $\sum F_H = 0$ AE = $910 \cos 30^\circ = 788.0831174 \text{ N}$ AE = 790 N (2 sf)
1 mark for equation based on vertical force components.	1	Node B $\sum F_v = 0$ BD = 1810 N BD = $910 \sin 30^\circ + 450$
1 mark for substitution.	1	BD = 1800 N (2 sf)
1 mark for nature.	1	BD is a strut
1 mark for BC.	1	BC = 2346.928844
1 mark for nature.	1	BC is a tie

11. (continued)



The structural design for the frame used to support the boom is shown.



Node N1 is in static equilibrium.

F1 is a strut, and F2 is a tie.

(c) (i) Write, in its simplest form, the equation for the vertical forces acting on N1 (include all forces and their angles).

1

(ii) Write, in its simplest form, the equation for the horizontal forces acting on N1 (include all forces and their angles).

1

11. (c) (continued)

(iii) Calculate the magnitude of the forces in members F1 and F2.

3

1 mark for presentation of equation shown is acceptable.	1	$\sum F_v = 0$ $F_1 \sin 45^\circ + F_2 \sin 60^\circ = 15 \cos 30^\circ$
1 mark for equation based on horizontal force components.	1	$F_1 \cos 45^\circ + F_2 \cos 60^\circ = 15 \cos 30^\circ$
1 mark for equation based on vertical force components.	1	$F_1 \sin 45^\circ - F_2 \sin 60^\circ = 15 \sin 30^\circ$
1 mark for F_1 with correct unit.	1	$F_1 = 16 \text{ kN}$ (2 sf)
1 mark for F_2 with correct unit.	1	$F_2 = 4.0 \text{ kN}$ (2 sf)
1 mark for appropriate substitution (other correct methods are acceptable).	1	$F_2 = (1.5 \sin 30^\circ - 15 \cos 30^\circ) / (-\sin 60^\circ - \cos 60^\circ)$ $F_2 = (-1.5 \sin 60^\circ - 15 \cos 60^\circ) / (-\sin 60^\circ - \cos 60^\circ)$ $F_2 = 4.0 \text{ kN}$ (2 sf)
1 mark for F_1 with correct unit.	1	$F_1 \sin 45^\circ - 4.0 \sin 60^\circ = 15 \sin 30^\circ$ $F_1 = 15.5055812$ $F_1 = 16 \text{ kN}$ (2 sf)
1 mark for nature.	1	BC is a tie
1 mark for BC.	1	BC = 2300 N (2 sf)
1 mark for substitution.	1	BC = $1800 \cos 30^\circ + 910 \cos 30^\circ$ BC = 2346.928844
1 mark for nature.	1	BD is a strut
1 mark for BD.	1	BD = 1800 N (2 sf)
1 mark for substitution.	1	BD = 1810 N BD = $910 \sin 30^\circ + 450$
1 mark for AE.	1	AE = 790 N (2 sf)
1 mark for AB.	1	AB = 910 N (2 sf)
1 mark for presentation of equation shown is acceptable.	1	Node A $\sum F_v = 0$ AB = 910 N (2 sf)
1 mark for equation based on horizontal force components.	1	Node B $\sum F_H = 0$ AE = $910 \cos 30^\circ = 788.0831174 \text{ N}$ AE = 790 N (2 sf)
1 mark for equation based on vertical force components.	1	Node B $\sum F_v = 0$ BD = 1810 N BD = $910 \sin 30^\circ + 450$
1 mark for substitution.	1	BD = 1800 N (2 sf)
1 mark for nature.	1	BD is a strut
1 mark for BC.	1	BC = 2346.928844
1 mark for nature.	1	BC is a tie